

H_∞ CONTROL-BASED ROBUST POWER SYSTEM STABILIZER FOR STABILITY ENHANCEMENT

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A robust H_∞ output feedback control approach is used to design power system stabilizers (PSS) for damping electrical power low-frequency oscillations over a wide range of operating conditions. Two H_∞ control schemes have been employed in the Single-Machine connected to an infinite bus (SMIB) system. The proposed stabilizers offer robust stability against different unknown loads, considered an external disturbance. The simulation results show good performance and stability enhancement. The effectiveness of the proposed approach is demonstrated by a comparative study with three other approaches: conventional PSS and robust power system stabilizers based on quantitative feedback theory (QFT).

NOMENCLATURE

Δv	Speed deviation (p.u.)
Δv_{\max}	Maximum speed deviation (p.u.)
δ	Power angle (rad)
δ_0	Initial power angle (rad)
ω	Rotor angular speed (rad/s)
ω_s	Synchronous rotor angular speed (rad/s)
θ	Power angle (deg)
D	Damping coefficient
E'_q	q-axis transient internal voltage (p.u.)
e_{d0}	Initial d-axis terminal voltage (p.u.)
E_{fd}	Rotor field voltage (p.u.)
e_{q0}	Initial q-axis terminal voltage (p.u.)
e_{t0}	Initial condition of terminal voltage (p.u.)
H	Inertia constant (s)
I_d, I_q	d and q-axis components of the generator stator current (p.u.)
I_g	Generator current (p.u.)
K_A	Automatic Voltage Regulator (AVR) gain
P, Q	Active and reactive powers (p.u.)
R_e, X_e	Line resistance and reactance (p.u.)
T'_{do}	d-axis transient open circuit time constant (s)
T_A	Automatic Voltage Regulator (AVR) time constant (s)
T_e	Electrical torque (p.u.)
T_m	Mechanical torque (p.u.)
V_∞	Infinite bus voltage (p.u.)
V_d, V_q	d and q-axis components of the terminal voltage (p.u.)
V_t	Terminal voltage (p.u.)
V_{ref}	Reference voltage (p.u.)
X'_d	d-axis transient reactance (p.u.)
X_d, X_q	d and q axis reactances (p.u.)

1. INTRODUCTION

Low-frequency electromechanical oscillations are a

significant problem for power system stability. The range of these oscillations is between 0.01 and 3Hz. The instability of the power system can lead to blackouts. Among additional controllers used to improve low-frequency oscillations damping is power system stabilizers (PSS), which are used to produce a supplementary damping torque signal through the automatic voltage regulator (AVR) [1].

These low-frequency electromechanical oscillations are associated with the small-signal stability of a power system. They are divided into an inter-area mode, a torsional mode, and a local mode [2].

The conventional power system stabilizer (CPSS) works efficiently at the nominal operating point and its performance decreases if the operating point changes [3]. In this case, the conventional PSS does not warrant the robustness of a power system for various ranges of operating conditions. To solve the robustness problem, the robust control design could guarantee robust stability for different operating conditions where the system is subject to external disturbance or parametric uncertainties [4].

The conventional power system stabilizer design based on a lead-lag compensator is one of the traditional techniques widely implemented in industrial AVR [5]. Besides, several optimization algorithms have been used to damp power system oscillations, one cites genetic algorithm [6], bio-inspired algorithms [7], particle swarm optimization (PSO) [8], cuckoo search optimization (CSO) technique [9] used to tune the PSS two lead-lag blocks, farmland fertility algorithm (FFA) [10], hyper-spherical search (HSS) optimization algorithm [11]. Therefore, nonlinear control methods have been designed as sliding mode control [12], and the artificial intelligence-based training and tuning methods have been used to design a PSS as a deep reinforcement learning-based method [13]. Furthermore, robust control theories have been employed in the design of robust power system stabilizers [14]. In [15], a linear matrix inequalities (LMI) technique is used to synthesize a robust pole placement for a single machine and multi-machines power system. In [16], an H_∞ feedback controller is applied to a non-linear dynamical model of a multi-machine power system.

In [17], the author used the μ -synthesis approach to design a coordinated control of PSS and additive High-voltage direct current (HVDC) damping controller in an

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ac/dc power system to attenuate intra-area mode oscillations.

Robust control techniques based on H_2 and H_∞ Norm have been developed in [3] using three weighting filters applied on a *SMIB*.

This paper proposes two H_∞ control schemes to design robust PSS and apply them to the *SMIB* system. The first scheme uses two weighting filters and the other uses four weighting filters and considers the system robustness in the *PSS* synthesis phase. The effectiveness of the proposed technique is demonstrated by a comparison of the obtained simulation results with three other techniques.

This paper is organized as follows. Section 2 gives a description of the *SMIB* mathematical model. Section 3 explains the control problem formulation. Section 4 presents the proposed resolution and the chosen weighting filters used in the proposed design. Section 5 shows simulation results, in which a comparative study is carried out between the *QFT*-based power system stabilizers, a conventional *PSS* [4], and the proposed control strategies. Finally, Section 6 ends this paper and gives some concluding observations.

2. SYSTEM MODEL

The system used in this study is a Single Machine connected to Infinite Bus (*SMIB*) through an external reactance X_e and external resistance R_e as shown in Fig. 1.

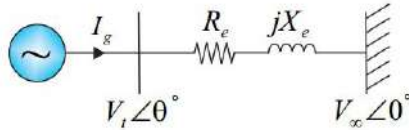


Fig. 1 – Diagram of *SMIB* system.

The model of the synchronous machine is described by the following equations:

$$\dot{\omega} = \frac{\omega_s}{2H} \left[T_m - (E'_q I_q + (X_q - X'_d) I_d I_q) - D(\omega - \omega_s) \right], \quad (1)$$

$$\dot{\delta} = (\omega - \omega_s), \quad (2)$$

$$\dot{E}'_q = \frac{1}{T_{do}} \left(E'_q + (X_d - X'_d) I_d - E_{fd} \right), \quad (3)$$

$$\dot{E}'_{fd} = \frac{1}{T_A} \left[-E_{fd} + K_A (V_{ref} - V_t) \right], \quad (4)$$

where all the model numerical values are given in the appendices. The *Heffron-Phillips* model of the *SMIB* system [18] is used in the proposed design as shown in Fig. 2.

The following linearized state-space model will be considered for the H_∞ *PSS* control design:

$$\begin{aligned} \Delta \dot{x} &= A \Delta x(t) + B_1 \Delta w(t) + B_2 \Delta u(t), \\ \Delta y(t) &= C \Delta x(t), \end{aligned} \quad (5)$$

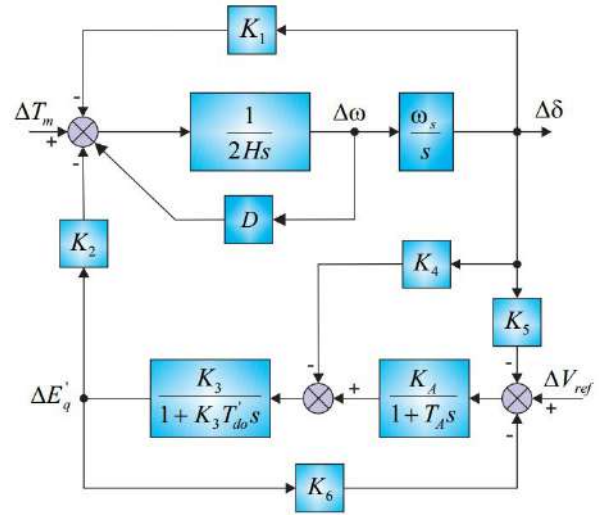


Fig. 2 – Scheme of Heffron-Phillips model.

where the matrices A , B , and C are defined as:

$$A = \begin{bmatrix} -1 & -K_4 & 0 & 1 \\ K_3 T_{do} & T_{do} & 0 & T_{do} \\ 0 & 0 & \omega_s & 0 \\ -K_2 & -K_1 & -D \omega_s & 0 \\ \frac{2H}{2H} & \frac{2H}{2H} & \frac{2H}{2H} & 0 \\ -K_A K_6 & -K_A K_5 & 0 & -1 \\ \frac{1}{T_A} & \frac{1}{T_A} & 0 & \frac{1}{T_A} \end{bmatrix}, \quad (6)$$

$$B = [B_1 | B_2] = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & \frac{1}{2H} & 0 \\ \frac{K_A}{T_A} & 0 & \frac{K_A}{T_A} \end{bmatrix}, \quad (7)$$

$$C = [0 \ 0 \ 1 \ 0], \quad (8)$$

where $\Delta x(t) = [\Delta E'_q \ \Delta \delta \ \Delta \omega \ \Delta E_{fd}]^T$ is the state vector, $\Delta w(t) = [\Delta V_{ref} \ \Delta T_m]^T$ is the vector of the external inputs (external disturbances), the control signal (the output of the power system stabilizer) is $\Delta u(t)$ and the system output signal is $\Delta y(t)$. The numerical values of the system parameters are calculated by the relationships given in the appendices.

3. CONTROL PROBLEM FORMULATION

Figure 3 illustrates the standard formulation of the problem, where $P(s)$ is a transfer matrix of the plant, $K(s)$ is the H_∞ *PSS*, w is the vector of the external inputs and disturbances, z is the vector of the outputs to be controlled, y is the measurement outputs and u is a control signal [19,20]. In this paper, the choice of the input/output of the standard problem is given by the external inputs w are the reference voltage variation ΔV_{ref} and the mechanical torque variation, ΔT_m . The measurement output y is the variation of the

speed deviation Δv . The control signal u is the H_∞ (HPSS) output ΔV_{pss} and the external outputs z depend to two proposed designs and they will be given in the next section.

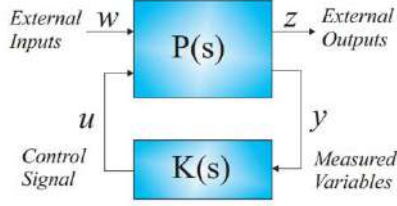


Fig. 3 – Standard control configuration.

The open-loop transfer matrix from $\begin{bmatrix} z \\ y \end{bmatrix}$ to $\begin{bmatrix} w \\ u \end{bmatrix}$ is:

$$\begin{bmatrix} z \\ y \end{bmatrix} = \begin{bmatrix} P_{11}(s) & P_{12}(s) \\ P_{21}(s) & P_{22}(s) \end{bmatrix} \begin{bmatrix} w \\ u \end{bmatrix}. \quad (9)$$

The linear fractional transformation (LFT) of the problem is given by:

$$T_{zw}(s) = P_{11}(s) + P_{12}(s)K(s)[I - P_{22}(s)K(s)]^{-1}P_{21}(s), \quad (10)$$

The H_∞ control problem is formulated as a minimization of the H_∞ norm γ such that:

$$\|T_{zw}(s)\|_\infty < \gamma. \quad (11)$$

The state space representation of the system can be given by the following equation:

$$\begin{bmatrix} \dot{x} \\ z \\ y \end{bmatrix} = \begin{bmatrix} A & B_1 & B_2 \\ C_1 & D_{11} & D_{12} \\ C_2 & D_{21} & D_{22} \end{bmatrix} \begin{bmatrix} x \\ w \\ u \end{bmatrix}, \quad (12)$$

where A is defined in (6) and

$$B_1 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & \frac{1}{2H} \\ \frac{K_A}{T_A} & 0 \end{bmatrix}, \quad B_2 = \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{K_A}{T_A} \end{bmatrix}, \quad D_{11} = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix},$$

$$C_1 = \begin{bmatrix} -K_6 & -K_5 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}, \quad D_{12} = \begin{bmatrix} 0 \\ 1 \end{bmatrix},$$

$$C_2 = [0 \ 0 \ 1 \ 0], \quad D_{21} = [0 \ 0], \quad D_{22} = [0].$$

4. H_∞ CONTROLLER RESOLUTION

4.1. CONTROLLER WITHOUT ROBUSTNESS WEIGHTING FILTER $W_3(s)$

To impose some dynamical performances in a H_∞ problem, it is necessary to include some weighting filters. In the first proposed design, two weighting filters $W_1(s)$ and $W_2(s)$ are included in the Plant as shown in Fig.4. In this case, the new considered external outputs are: z_1 and z_2 , where z_1 is the measurement output $y(t)$ (speed deviation Δv) connected to

the error weighting filter W_1 ($z_1 = W_1(s) \cdot y$) and z_2 is the control signal $u(t)$ (PSS voltage output ΔV_{pss}) connected to control weighting filter W_2 ($z_2 = W_2(s) \cdot u$).

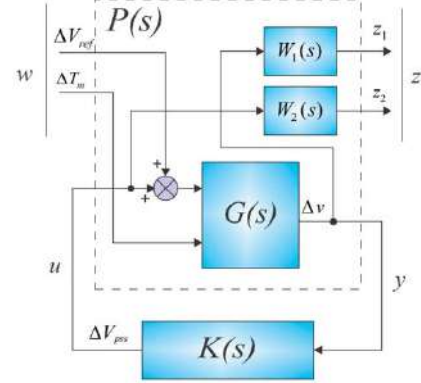


Fig. 4 – Filters augmentation of the system without using $W_3(s)$.

The choice of these weighting filters is an important step, an error weighting filter W_1 is chosen to limit the peak of the speed deviation Δv

$$W_1(s) = \frac{1}{\Delta v_{\max}}. \quad (13)$$

The control weighting filter $W_2(s)$ (given by the equation 14) is chosen to accelerate the convergence of the HPSS output ΔV_{pss} to zero and therefore, the settling time of speed deviation Δv will be reduced.

$$W_2(s) = \frac{w_b}{s + w_b \varepsilon}, \quad (14)$$

where w_b and ε are the tuning parameters. The following parameters values satisfy the design requirements for the nominal operating condition ($P = 0.8$ p.u., $Q = 0.4$ p.u. and $X_e = 0.2$ p.u.): $\Delta v_{\max} = 10^{-3}$, $w_b = 62.5$ and $\varepsilon = 10^{-4}$.

To facilitate the PSS implementation, the obtained HPSS can be reformulated in the following form (like a conventional PSS structure with additional filter):

$$K(s) = \frac{K_s (s + T_1)(s + T_2)(s^2 + a_1 s + b_1)}{(s + T_3)(s + T_4)(s^2 + a_2 s + b_2)}. \quad (15)$$

The parameters numerical values of the obtained HPSS1 controller are given in Table 1.

Table 1
HPSS1 parameters

$K_s = -2.12 \cdot 10^7$	$T_3 = 223.4$	$b_1 = 160.2$
$T_1 = -20.86$	$T_4 = 5 \cdot 10^{-7}$	$a_2 = 5657$
$T_2 = 6.25 \cdot 10^{-3}$	$a_1 = 23.65$	$b_2 = 9.23 \cdot 10^6$

Remark: it is noted that the order of the designed HPSS1 is equal to the sum of the system order and the weighting filter order. With a cancellation of a zero and a pole, the proposed design leads to an HPSS1 of order 4.

4.2. CONTROLLER WITH ROBUSTNESS WEIGHTING FILTER $W_3(s)$ AND VOLTAGE ERROR WEIGHTING FILTER $W_{dV}(s)$

In the second design proposed in this paper, four weighting filters are included in the Plant as shown in Fig.5. In this case, in addition to the external outputs z_1 and z_2 proposed in the previous design, two other outputs z_3 and z_4 are considered, where z_3 is the voltage error ($V_{dV} = \Delta V_{ref} - \Delta V_t$) connected to the weighting filter W_{dV} ($z_3 = W_{dV}(s)V_{dV}$) and z_4 is the terminal voltage ΔV_t connected to the robustness weighting filter W_3 ($z_4 = W_3(s)\Delta V_t$). The weighting filters are given in the following: $W_1(s) = 2.5 \cdot 10^5$, $W_2(s) = \frac{1}{0.1}$, $W_3(s) = \frac{600}{s+6}$, $W_4(s) = \frac{2 \cdot 10^4}{s+0.002}$. The obtained *HPSS2* controller is designed to consider several operating conditions (P, Q, X_e) through the weighting filters, can be reformulated as follows:

$$K(s) = \frac{K_s (s+T_1)(s+T_2)(s+T_3)(s^2+a_1s+b_1)}{(s+T_4)(s+T_5)(s+T_6)(s^2+a_2s+b_2)}, \quad (16)$$

where its parameters are given in Table 2.

Table 2
HPSS2 Parameters

$K_s = 7.44 \cdot 10^6$	$T_4 = 787.20$	$a_1 = 26.13$
$T_1 = 6.00$	$T_5 = 14.08$	$b_1 = 197.40$
$T_2 = 4.03$	$T_6 = 6.00$	$a_2 = 188.00$
$T_3 = -0.01$	$T_7 = 5.06 \cdot 10^{-3}$	$b_2 = 1.70 \cdot 10^4$

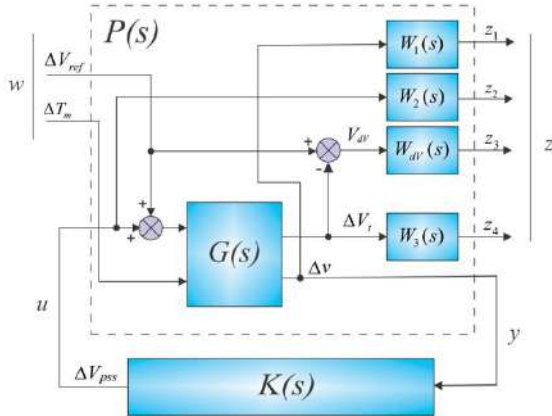


Fig. 5 – Filters augmentation of the system with using $W_3(s)$ and $W_{dV}(s)$.

5. SIMULATION RESULTS

To prove the robustness and effectiveness of the proposed H_∞ PSS controllers (called *HPSS* in the following figures), several studies have been performed on the SMIB system at different operating conditions, where the parameters of the system components are given in the Appendices. Furthermore, a comparative study is carried out with three methods: conventional PSS [5] (called *CPSS* in the following figures) and two other methods based on

Quantitative Feedback Theory (simplex and Nonlinear programming methods) [4] (called in the following figures *QFT1-PSS* and *QFT2-PSS* respectively). Three different operating conditions have been considered with respect to the active power P , the reactive power Q , and the reactance of the transmission line X_e . A 5% step disturbance at the *AVR* voltage reference input is applied for the following three operating conditions:

- 1st test: $P = 0.8$ p.u., $Q = 0.4$ p.u. and $X_e = 0.2$ p.u.
- 2nd test: $P = 0.8$ p.u., $Q = 0.0$ p.u. and $X_e = 0.6$ p.u.
- 3rd test: $P = 1.0$ p.u., $Q = 0.5$ p.u. and $X_e = 0.7$ p.u.

The comparison of the simulation results obtained with conventional PSS (*CPSS*) and *QFT*-based PSSs (*QFT1-PSS* and *QFT2-PSS*) shows that the proposed *HPSS* stabilizers achieve better performances.

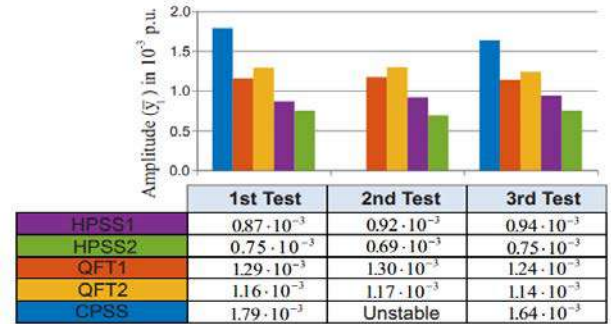


Fig. 6 – Comparison of the first oscillation amplitude of proposed PSSs conventional PSS and *QFT*-based PSSs.

Figures 6, 7, and 8 show a quantitative comparison of the proposed PSSs with conventional PSS and *QFT*-based PSSs, where, the parameter \bar{y}_1 represents the first oscillation amplitude of the system response, \bar{y}_2 is the amplitude of the second oscillation and t_s is the settling time for $|y| < 0.0001$, where y is the speed variation.

Figures 9, 10, and 11 present respectively the simulation results of rotor angular speed variation Δv and the power system stabilizer control signal ΔV_{pss} for the 1st, 2nd, and 3rd tests. As can be observed from these figures, the first oscillation amplitudes of the proposed PSSs (*HPSS*) are less than the other controllers in all the performed tests.

The *QFT*-based PSSs have two other oscillations before the stability in the 2nd and the 3rd tests, whereas the conventional PSS cannot stabilize the system in the 2nd test and it has many oscillations in the 3rd test, while the first proposed PSS (*HPSS1*) has only one oscillation in all the performed tests. It is noted that the first oscillation of the second proposed PSS (*HPSS2*) is smaller than all the other PSS. Furthermore, the amplitude of its second oscillation is better than *QFT*-based PSSs. The settling time of the first proposed PSS is less than half the value of the others in the 2nd and the 3rd tests.

The second proposed design has a good settling time in the 2nd and the 3rd tests compared to *QFT*-based PSSs and conventional PSS. At the end, it is noted that the control signal of the proposed *HPSS* is in the range $-0.1 < V_{pss} < 0.1$ in all the performed tests as recommended by [5].

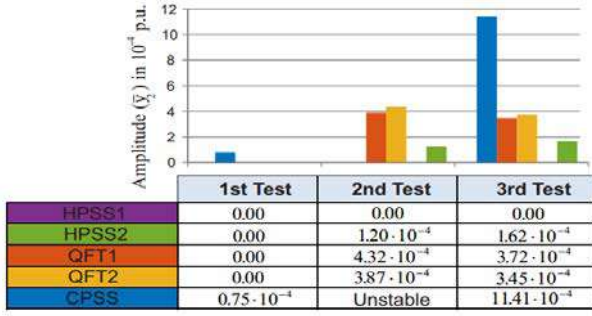


Fig. 7 – Comparison of the second oscillation amplitude of proposed PSSs conventional PSS and QFT-based PSSs.

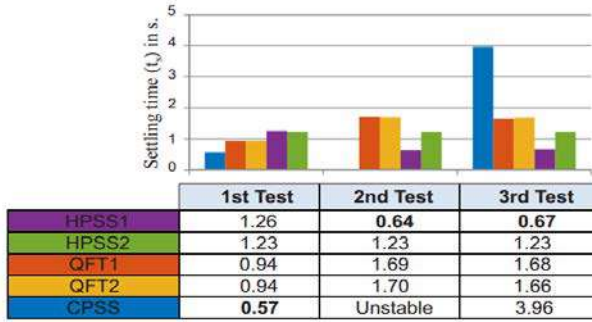


Fig. 8 – Comparison of the settling time obtained with proposed PSSs, QFT1 and QFT2 PSSs and a conventional PSS.

6. CONCLUSIONS

In this paper, a robust power system stabilizer using H_∞ control approach is applied to a Single Machine connected to an Infinite Bus (SMIB) system. The main objective is to enhance the stability and the robustness of the SMIB against different unknown loads, external disturbances (Steps in the reference voltage or in the applied torque) and the variation of the external reactance X_e . The first proposed HPSS1 has a simple architecture, simple weighting filters, and good performance. The second proposed design HPSS2 has good robustness and good performance compared to conventional PSS and QFT-PSSs.

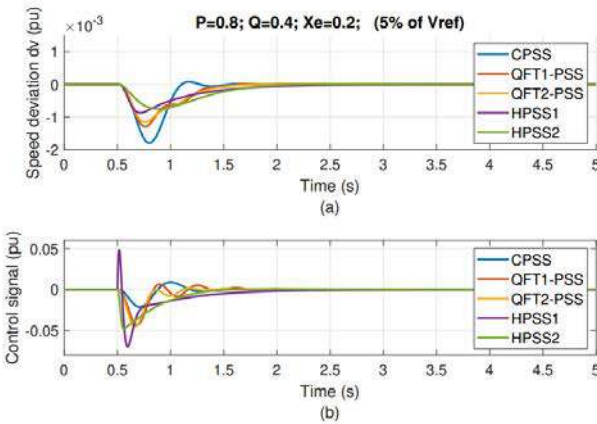


Fig. 9 – SMIB response to a 5% step disturbance at the voltage reference input, (1st test: $P = 0.8$, $Q = 0.4$ and $X_e = 0.2$).

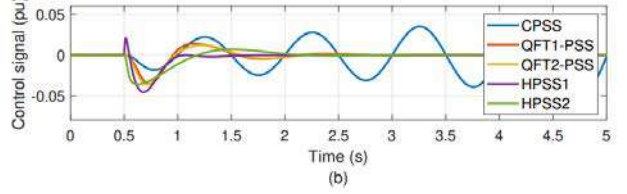
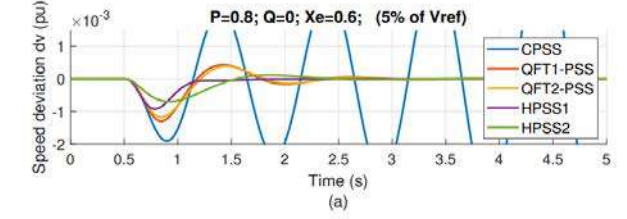


Fig. 10 – SMIB response to a 5% step disturbance at the voltage reference input, (2nd test: $P = 0.8$, $Q = 0.0$ and $X_e = 0.6$).

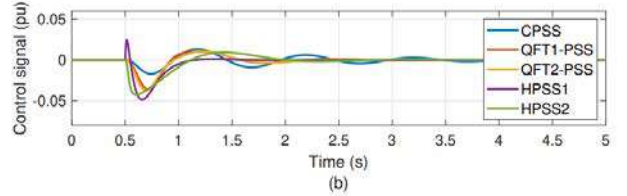
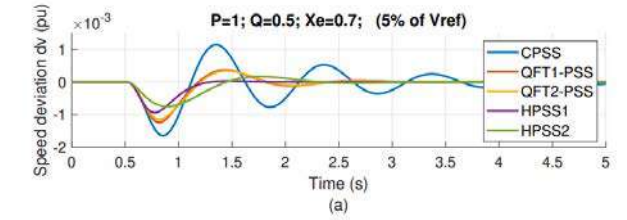


Fig. 11 – SMIB response to a 5% step disturbance at the voltage reference input, (3rd test: $P = 1.0$, $Q = 0.5$ and $X_e = 0.7$).

The simulation results confirm the great benefit of a robust H_∞ PSS output feedback controller compared to the QFT-based PSSs regarding the time response, the speed deviation dynamic, and the disturbance rejection. As a perspective, the proposed design will be applied to a multi-machine system to damp inter-area oscillations.

APPENDIX

A. THE SMIB EQUATIONS

In this section, the relationships for a SMIB are defined as in [21]. The expression used to calculate the system constants K_1 to K_6 are defined as follows:

$$K_1 = \frac{X_q - X'_d}{X_e + X'_d} I_{q0} V_\infty \sin \delta_0 + \frac{V_{q0} V_\infty \cos \delta_0}{X_e + X_q},$$

$$K_2 = \frac{V_\infty}{X_e + X'_d} \sin \delta_0, \quad K_3 = \frac{X'_d + X_e}{X_d + X_e},$$

$$K_4 = \frac{X_d - X'_d}{X_e + X'_d} V_\infty \sin \delta_0,$$

$$K_5 = \frac{X_q}{X_e + X_q} \frac{e_{d0}}{e_{t0}} V_\infty \cos \delta_0 - \frac{X'_d}{X_e + X'_d} \frac{e_{q0}}{e_{t0}} V_\infty \sin \delta_0,$$

$$K_6 = \frac{X_e}{X_e + X'_d} \frac{e_{q0}}{e_{t0}}$$

B. THE SMIB DATA

The parameters in per unit of the SMIB [4] presented in Fig.1 are given in Table B.3.

Table B.3
The system data

$X_d = 2.0 p.u.$	$T'_{do} = 4.18s$	$V_\infty = 1 p.u.$
$X_q = 1.91 p.u.$	$K_A = 50 p.u.$	$H = 3.25s$
$X'_d = 0.244 p.u.$	$T_A = 0.05s$	$\omega_s = 314 rad/s$

C. THE CONVENTIONAL PSS AND QFT-PSS DATA

The transfer function of the CPSS is given as follows:

$$K_0(s) = K_s \frac{(s + T_1)^2}{(s + T_2)^2},$$

where K_s , T_1 and T_2 are respectively the PSS gain and its parameters. The CPSS and QFT- PSSs parameters obtained by [4] are given in the Table C.5.

Table C.5
CPSS, QFT1 and QFT2 Parameters, [4]

Controller Parameters	Design Method		
	QFT1	QFT2	CPSS
K_s	13.88	16.22	5.5
T_1	0.1785	0.1542	0.1732
T_2	0.0614	0.0440	0.0577

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