

# IMPROVED ADAPTIVE NONLINEAR CONTROL FOR VARIABLE SPEED WIND-TURBINE FED BY DIRECT MATRIX CONVERTER

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**Keywords:** Input-output linearizing and decoupling control (I/OLDC); Doubly fed induction generator (DFIG); Matrix converter (MC); Wind energy conversion system (WECS); Model reference adaptive control (MRAC).

This paper proposes a robust decoupling power algorithm based on a doubly fed induction generator (DFIG) for variable speed wind-turbine (WT). The DFIG rotor circuit is fed by the direct matrix converter (DMC), which presents several features such as no need to the dc-bus voltage, sinusoidal supply, rotor side waveforms, bidirectional power flow, and adjustable input power factor. The 18 bidirectional switches are controlled using the Venturini modulation technique. On the other hand, the DFIG stator circuit is connected directly to the grid. The nonlinear control strategy based on feedback linearization is applied to control the stator power ( $P_s$  and  $Q_s$ ) independently using the rotor quadrature and direct currents ( $i_{rq}$  and  $i_{rd}$ ), which present the images of the previous stator powers. Some limitations appear in the power algorithm using the conventional pi controller, especially in power tracking, error, and quality. In this context, the model reference adaptive controller (MRAC) presents an alternative solution, a robust and efficient controller proposed instead of the pi controllers to control stator powers. Finally, the simulation results confirm that the proposed algorithm could work under hard conditions and demonstrate that the wind energy conversion system (WECS) provides enhanced dynamic responses in transient and steady states and good power quality delivered to the grid.

## 1. INTRODUCTION

Among several renewable energies, wind energy is considered one of the best promising renewable energy in the world. In the last few years, the installed wind plants worldwide have grown more than 30 % [1,2]. The doubly-fed induction generator (DFIG) is the most useful generator for wind turbine systems due to the various features: maximum power point tracking (MPPT) strategy, which depends on the variable speed operation, decoupled power control, smaller converter prices, and reduced power losses [3,4].

The conventional back-to-back two-level converters are the most used power electronic interface for wind system power generation [5]. However, they need a wide source filter inductor resulting in low reliability, high price, and wide size [6,7]. Nowadays, matrix converters (MC) are more popular due to several interesting gains, like sinusoidal input/output waveforms, bi-directionality power flow, input unity power

factor, and the absence of the dc link [6–10]. A direct matrix converter (DMC) can be used to control the DFIG instead of the classical back-to-back converters, as depicted in (Fig. 1). The DMC doesn't require costly energy storage elements, and its implementation scheme is more accessible than that used by two stages power conversion [11].

Recently, vector control (VC) has been the most used control algorithm for a wind turbine-driven DFIG [12,13]. In literature, many control strategies of DFIG have been discussed, such as backstepping control [14,15], fractional order sliding mode control (SMC) [16], high order SMC [17], model predictive direct power control (MPDPC) [18]. Some authors focus their contributions on a simple and robust control based on independent control of rotor currents, named input-output linearizing and decoupling control (I/OLDC) [19], which could work under different operating modes.

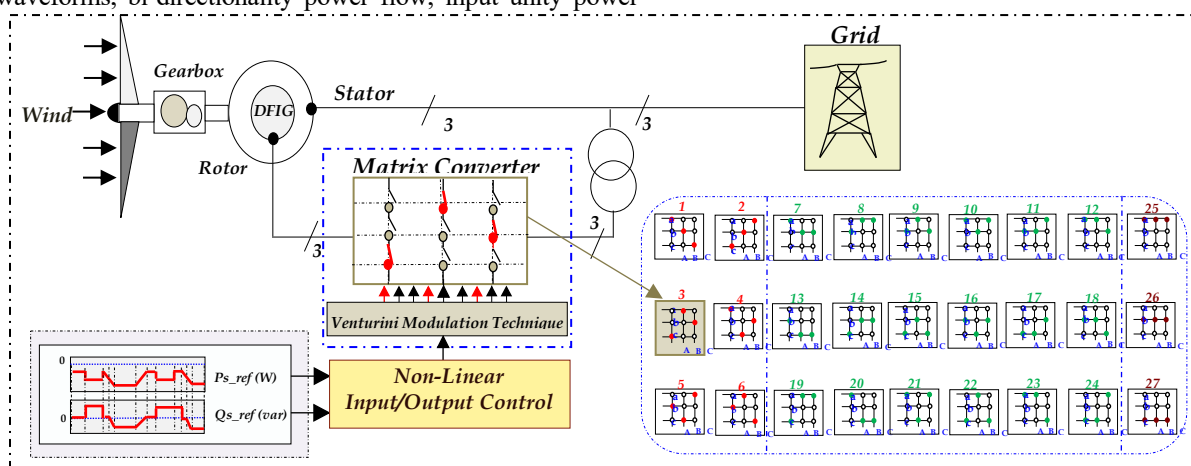


Fig. 1 – WECS based on DFIG-Matrix converter using nonlinear control.

In this work, the nonlinear approach is proposed to control d-q axis rotor currents of the DFIG. Some researchers used

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the PI classical regulators to control the stator powers [20]. Several limitations appear such as: dynamic response, static power error, and delivered power quality. In this context, a robust and adaptive controller named model reference adaptive control (MRAC) [21–24] is applied; instead, the classical PI regulators operate under different modes (sub or super-synchronous mode under random wind speed) to avoid the previous drawbacks.

The main contribution of this paper is the investigation of the improved wind-power algorithm based on nonlinear theory and MRAC adaptive controller (Fig. 1) to guarantee high wind-power performances; different hard tests are proposed.

This paper is structured as follows; firstly, the matrix converter (MC) modeling is presented in section 2. Sections 3 and 4 present a mathematical model of the DFIG and the proposed I/OLDC. In section 5, simulation results are discussed. Finally, the reported work is concluded.

## 2. MATRIX CONVERTER (MC) MODEL

Three-phase MC connects the three-phase ac voltages on the input side to the three-phase voltages on the output side by a 3\*3 Matrix using bidirectional switches. Consequently, there are only  $3^3 = 27$  possible states of operation for the switches [25–27]. The output currents and voltages are presented in Table 1. The schematic models of the MC and output voltage waveform (with the zoom) are shown in Fig. 2 and Fig. 3, respectively.

Table 1  
27 States of Matrix converter.

Possible States:	V <sub>A</sub>	V <sub>B</sub>	V <sub>C</sub>	V <sub>AB</sub>	V <sub>BC</sub>	V <sub>CA</sub>	I <sub>a</sub>	I <sub>b</sub>	I <sub>c</sub>
1	V <sub>a</sub>	V <sub>b</sub>	V <sub>c</sub>	V <sub>ab</sub>	V <sub>bc</sub>	V <sub>ca</sub>	I <sub>A</sub>	I <sub>B</sub>	I <sub>C</sub>
2	V <sub>a</sub>	V <sub>c</sub>	V <sub>b</sub>	-V <sub>ca</sub>	-V <sub>bc</sub>	-V <sub>ab</sub>	I <sub>A</sub>	I <sub>C</sub>	I <sub>B</sub>
3	V <sub>b</sub>	V <sub>a</sub>	V <sub>c</sub>	-V <sub>ab</sub>	-V <sub>ca</sub>	-V <sub>bc</sub>	I <sub>B</sub>	I <sub>A</sub>	I <sub>C</sub>
4	V <sub>b</sub>	V <sub>c</sub>	V <sub>a</sub>	V <sub>bc</sub>	V <sub>ca</sub>	V <sub>ab</sub>	I <sub>C</sub>	I <sub>A</sub>	I <sub>B</sub>
5	V <sub>c</sub>	V <sub>a</sub>	V <sub>b</sub>	V <sub>ca</sub>	V <sub>ab</sub>	V <sub>bc</sub>	I <sub>B</sub>	I <sub>C</sub>	I <sub>A</sub>
6	V <sub>c</sub>	V <sub>b</sub>	V <sub>a</sub>	-V <sub>bc</sub>	-V <sub>ca</sub>	-V <sub>ab</sub>	I <sub>C</sub>	I <sub>B</sub>	I <sub>A</sub>
7	V <sub>a</sub>	V <sub>b</sub>	V <sub>b</sub>	V <sub>ab</sub>	0	-V <sub>ab</sub>	I <sub>A</sub>	-I <sub>A</sub>	0
8	V <sub>b</sub>	V <sub>a</sub>	V <sub>a</sub>	-V <sub>ab</sub>	0	V <sub>ab</sub>	-I <sub>A</sub>	I <sub>A</sub>	0
9	V <sub>b</sub>	V <sub>c</sub>	V <sub>c</sub>	V <sub>bc</sub>	0	-V <sub>bc</sub>	0	I <sub>A</sub>	-I <sub>A</sub>
10	V <sub>c</sub>	V <sub>b</sub>	V <sub>b</sub>	-V <sub>bc</sub>	0	V <sub>bc</sub>	0	-I <sub>A</sub>	I <sub>A</sub>
11	V <sub>c</sub>	V <sub>a</sub>	V <sub>a</sub>	V <sub>ca</sub>	0	-V <sub>ca</sub>	-I <sub>A</sub>	0	I <sub>A</sub>
12	V <sub>a</sub>	V <sub>c</sub>	V <sub>c</sub>	-V <sub>ca</sub>	0	V <sub>ca</sub>	I <sub>A</sub>	0	-I <sub>A</sub>
13	V <sub>b</sub>	V <sub>a</sub>	V <sub>b</sub>	-V <sub>ab</sub>	V <sub>ab</sub>	0	I <sub>B</sub>	-I <sub>B</sub>	0
14	V <sub>a</sub>	V <sub>b</sub>	V <sub>a</sub>	V <sub>ab</sub>	-V <sub>ab</sub>	0	-I <sub>B</sub>	I <sub>B</sub>	0
15	V <sub>c</sub>	V <sub>b</sub>	V <sub>c</sub>	-V <sub>bc</sub>	V <sub>bc</sub>	0	0	I <sub>B</sub>	-I <sub>B</sub>
16	V <sub>b</sub>	V <sub>c</sub>	V <sub>b</sub>	V <sub>bc</sub>	-V <sub>bc</sub>	0	0	-I <sub>B</sub>	I <sub>B</sub>
17	V <sub>a</sub>	V <sub>c</sub>	V <sub>a</sub>	-V <sub>ca</sub>	V <sub>ca</sub>	0	-I <sub>B</sub>	0	I <sub>B</sub>
18	V <sub>c</sub>	V <sub>a</sub>	V <sub>c</sub>	V <sub>ca</sub>	-V <sub>ca</sub>	0	I <sub>B</sub>	0	-I <sub>B</sub>
19	V <sub>b</sub>	V <sub>b</sub>	V <sub>a</sub>	0	-V <sub>ab</sub>	V <sub>ab</sub>	I <sub>C</sub>	-I <sub>C</sub>	0
20	V <sub>a</sub>	V <sub>a</sub>	V <sub>b</sub>	0	V <sub>ab</sub>	-V <sub>ab</sub>	-I <sub>C</sub>	I <sub>C</sub>	0
21	V <sub>c</sub>	V <sub>c</sub>	V <sub>b</sub>	0	-V <sub>bc</sub>	V <sub>bc</sub>	0	I <sub>C</sub>	-I <sub>C</sub>
22	V <sub>b</sub>	V <sub>b</sub>	V <sub>c</sub>	0	V <sub>bc</sub>	-V <sub>bc</sub>	0	-I <sub>C</sub>	I <sub>C</sub>
23	V <sub>a</sub>	V <sub>a</sub>	V <sub>c</sub>	0	-V <sub>ca</sub>	V <sub>ca</sub>	-I <sub>C</sub>	0	I <sub>C</sub>
24	V <sub>c</sub>	V <sub>c</sub>	V <sub>a</sub>	0	V <sub>ca</sub>	-V <sub>ca</sub>	I <sub>C</sub>	0	-I <sub>C</sub>
25	V <sub>a</sub>	V <sub>a</sub>	V <sub>a</sub>	0	0	0	0	0	0
26	V <sub>b</sub>	V <sub>b</sub>	V <sub>b</sub>	0	0	0	0	0	0
27	V <sub>c</sub>	V <sub>c</sub>	V <sub>c</sub>	0	0	0	0	0	0

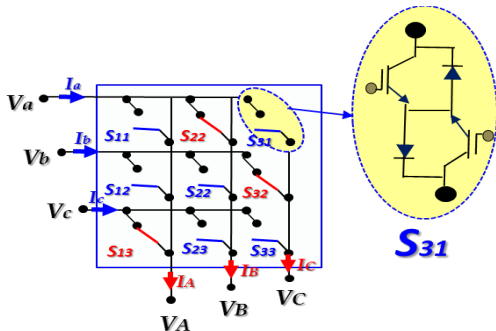


Fig. 2 – Schematic model of Matrix converter (MC).

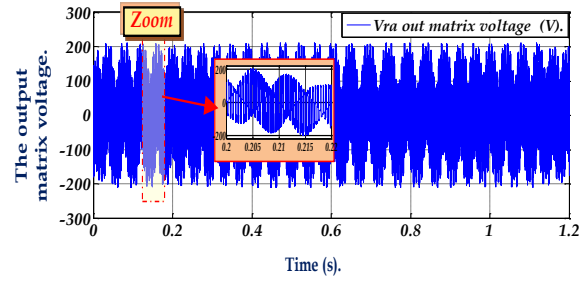


Fig. 3 – The output phase voltage of the Matrix converter.

## 3. MATHEMATICAL MODEL OF THE DFIG

The mathematical model of the DFIG is presented under the d-q Park reference [1, 21,22]. The stator/rotor voltage and fluxes equations are presented respectively:

$$\begin{cases} V_{sd} = R_s I_{sd} + \frac{d}{dt} \phi_{sd} - \omega_s \phi_{sq} \\ V_{sq} = R_s I_{sq} + \frac{d}{dt} \phi_{sq} - \omega_s \phi_{sd} \\ V_{rd} = R_r I_{rd} + \frac{d}{dt} \phi_{rd} - (\omega_s - \omega) \phi_{rq} \\ V_{rq} = R_r I_{rq} + \frac{d}{dt} \phi_{rq} - (\omega_s - \omega) \phi_{rd} \end{cases} \quad (1)$$

$$\begin{cases} \phi_{sd} = L_s I_{sd} + L_m I_{rd} \\ \phi_{sq} = L_s I_{sq} + L_m I_{rq} \\ \phi_{rd} = L_r I_{rd} + L_m I_{sd} \\ \phi_{rq} = L_r I_{rq} + L_m I_{sq} \end{cases} \quad (2)$$

The electromagnetic torque ( $T_{em}$ ) is presented as follows:

$$\begin{cases} T_{em} = P L_m (I_{rd} I_{sq} - I_{rq} I_{sd}) \\ T_{em} - T_r = J \frac{d}{dt} \Omega + f \Omega \end{cases} \quad (3)$$

where:  $\phi_{sd}, \phi_{sq}$  and  $\phi_{rd}, \phi_{rq}$  are stator and rotor flux components, respectively,  $V_{sd}, V_{sq}$  and  $V_{rd}, V_{rq}$  are stators and rotor voltage components, respectively.  $R_s, R_r$  and  $L_s, L_r$  are stator and rotor resistances and inductances respectively.  $L_m$  is mutual inductance,  $\sigma$  is leakage factor,  $P$  is number of pole pairs,  $\omega_s$  is the stator pulsation,  $\omega$  is the rotor pulsation,  $f$  is the friction coefficient, and  $S$  is the slip,  $T_{em}$  and  $T_r$ : are the electromagnetic and the load torques,  $J$ : is total inertia and  $\Omega$ : is mechanical speed.

The DFIG mathematical model is developed in the synchronous reference frame. This work's d-axis is aligned with the stator flux vector (Fig. 4).

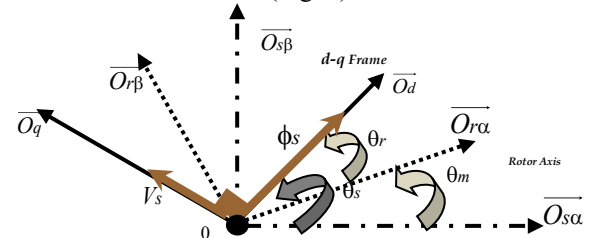


Fig. 4 – Stator flux vector in the d-q reference.

In this work, the stator resistance is neglected. In the steady state, the simplified model is described as follows:

$$V_{sd} = 0 \text{ and } V_{sq} = V_s \cong \omega_s \phi_s \quad (4)$$

$$\phi_s = L_s I_{sd} + L_m I_{rd} \quad (5)$$

$$0 = L_s I_{sq} + L_m I_{rq} \quad (6)$$

From (5) and (6), the equations of stator/rotor currents:

$$I_{sd} = \frac{\phi_s}{L_s} - \frac{L_m}{L_s} I_{rd} \quad (7)$$

$$I_{sq} = -\frac{L_m}{L_s} I_{rq} \quad (8)$$

The DFIG powers are presented as:

$$P_s = V_{sd} I_{sd} + V_{sq} I_{sq} \quad (9)$$

$$Q_s = V_{sq} I_{sd} - V_{sd} I_{sq} \quad (10)$$

By applying the d-a reference synchronous frame, the DFIG power equations can be defined:

$$P_s = V_s I_{sq} \quad (11)$$

$$Q_s = V_s I_{sd} \quad (12)$$

Replacing the d-q axis stator currents in expressions (11) and (12), we obtain:

$$\begin{cases} P_s = -V_s \frac{L_m}{L_s} I_{rq} \\ Q_s = \frac{V_s^2}{\omega_s L_s} - V_s \frac{L_m}{L_s} I_{rd} \end{cases} \quad (13)$$

The rotor quadrature component current  $I_{rq}$  controls the stator real power ( $P_s$ ), and the reactive power is controlled by the direct component  $I_{rd}$  as illustrated in the Fig. 5.

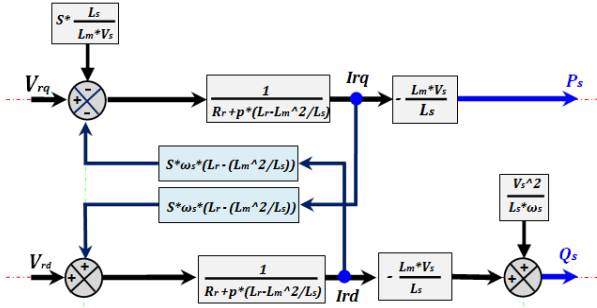


Fig. 5 – The doubly fed induction generator simplified model.

#### 4. PROPOSED INPUT/OUTPUT LINEARIZING AND DECOUPLING CONTROL BASED ON MRAC

Given the system by [19,20] as shown in Fig. 6:

$$\begin{cases} \dot{x} = f_n(x) + g_u u \\ y = h(x) \end{cases} \quad (14)$$

where  $x$  is state vector;  $u$  and  $y$  are respectively the input and output;  $f_n$ ,  $g$  and  $h$  are smooth vector fields and scalar function respectively.

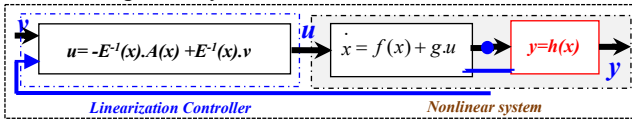


Fig.6 –The input-output linearizing control schematic.

To get the linearization of MIMO system, the  $y$  output is differentiated until the inputs appear.

$$\dot{y} = L_f h(x) + L_g(x) u \quad (15)$$

Where:  $L_f h(x) = \frac{\partial h}{\partial x} \cdot f_n(x)$  and  $L_g h(x) = \frac{\partial h}{\partial x} g(x)$ ; represent

Lie derivatives of  $h(x)$  with respect to  $f_n(x)$  and  $g(x)$  respectively.

If  $L_g h(x) = 0$  then the input  $u$  don't appear and the output is differentiated respectively.

$$y^{(r)} = L_f^r h(x) + L_g^{r-1} h(x) u \quad (16)$$

Where “ $r$ ” is the relative rank of “ $y$ ”. If we perform the above procedure for each input “ $y_i$ ”, we get a total of “ $m$ ” equations in the above form, which can be written completely as:

$$\begin{bmatrix} y_1^{(r)} \\ \dots \\ y_m^{(rm)} \end{bmatrix} = A(x) + E(x) \begin{bmatrix} u_1 \\ \dots \\ u_m \end{bmatrix} \quad (17)$$

where the  $m \times m$  matrix  $E(x)$  is defined as:

$$E(x) = \begin{bmatrix} L_{g1} L_f^{r-1} h_1 & \dots & L_{gm} L_f^{r-1} h_1 \\ \dots & \dots & \dots \\ L_{g1} L_f^{rm-1} h_m & \dots & L_{gm} L_f^{rm-1} h_m \end{bmatrix} \quad (18)$$

$$A(x) = \begin{bmatrix} L_f^r h_1 & \dots & L_f^{rm} h_m \end{bmatrix}^T \quad (19)$$

$E(x)$  is the decoupling matrix for the system. If  $E(x)$  is nonsingular, then the original input  $u$  is controlled by the coordinate transformation:

$$u = -E^{-1}(x)A(x) + E^{-1}(x)v = E^{-1}(x)[v - A(x)] \quad (20)$$

$$\text{Where } v = [v_1 \dots v_m]^T$$

Substituting (19) into (17) obtains a linear differential relation between the output  $y$  and the new input  $v$ .

$$\begin{bmatrix} y_1^{(r)} \\ \dots \\ y_m^{(rm)} \end{bmatrix} = \begin{bmatrix} v_1 \\ \dots \\ v_m \end{bmatrix} \quad (21)$$

According (7) and (8), the direct and quadrature components of the stator and the rotor currents are linearly dependent respectively, thus we choose state vectors of the DFIG as follows:

$$x = [x_1 \ x_2]^T = [I_{rd} \ I_{rq}]^T \quad (22)$$

By substituting (2), (5), (6), (7) and (8) to (1): the rotor voltage d-q components ( $V_{rd}$  and  $V_{rq}$ ) are presented as follows:

$$V_{rd} = R_r I_{rd} + \sigma L_r \frac{d}{dt} I_{rd} - (\omega_s - \omega_r) \sigma L_r I_{rq} \quad (23)$$

$$V_{rq} = R_r I_{rq} + \sigma \frac{d}{dt} I_{rq} - (\omega_s - \omega_r) \sigma L_r I_{rd} \quad (24)$$

where:  $\sigma = 1 - \frac{L_m^2}{L_s L_r}$

Arranging (23) and (24) in the form of (14)

$$\frac{d}{dt} I_{rd} = -\frac{R_r}{\sigma L_r} I_{rd} + \frac{1}{L_r} (\omega_s - \omega_r) I_{rq} + \frac{V_{rq}}{\sigma L_r} \quad (25)$$

$$\frac{d}{dt} I_{rq} = -\frac{R_r}{\sigma} I_{rq} - (\omega_s - \omega_r) L_r I_{rd} + \frac{V_{rq}}{\sigma} \quad (26)$$

Defining the input of the DFIG system:

$$u = [u_1 \ u_2]^T = [V_{rd} \ V_{rq}]^T \quad (27)$$

From (40) and (41), we have:

$$f_{n1} = -\frac{R_r}{\sigma L_r} I_{rd} + \frac{1}{L_r} (\omega_s - \omega_r) I_{rq} \quad (28)$$

$$f_{n2} = -\frac{R_r}{\sigma} I_{rq} - L_r (\omega_s - \omega_r) I_{rd} \quad (29)$$

$$g = \begin{bmatrix} 1 & 0 \\ \sigma L_r & 1 \\ 0 & \frac{1}{\sigma} \end{bmatrix} \quad (30)$$

The selected outputs of the nonlinear system are defined by the stator active ( $P_s$ ) and reactive ( $Q_s$ ) powers:

$$y = \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} P_s \\ Q_s \end{bmatrix} = \begin{bmatrix} V_{sd} I_{sd} + V_{sq} I_{sq} \\ V_{sq} I_{sd} - V_{sd} I_{sq} \end{bmatrix} \quad (31)$$

From (7), (8) and (31):

$$y_1 = \frac{\phi_s}{L_s} V_{sd} - \frac{L_m}{L_s} (V_{sd} I_{rd} - V_{sq} I_{rq}) \quad (32)$$

$$y_2 = \frac{\phi_s}{L_s} V_{sq} - \frac{L_m}{L_s} (V_{sq} I_{rd} - V_{sd} I_{rq}) \quad (33)$$

Differentiating (32) and (33) until an input appears:

$$\dot{y}_1 = \frac{V_{sd}}{L_s} (\dot{\phi}_s - L_m \dot{I}_{rd}) - \frac{L_m}{L_s} \dot{V}_{sq} I_{rq} - \frac{L_m}{L_s} (V_{sd} \dot{f}_{n1} - V_{sq} \dot{f}_{n2}) - \frac{L_m V_{sd}}{\sigma L_s L_r} V_{rd} - \frac{L_m V_{sq}}{\sigma L_s} V_{rq} \quad (34)$$

$$\dot{y}_2 = \frac{V_{sq}}{L_s} (\dot{\phi}_s - L_m \dot{I}_{rd}) - \frac{L_m}{L_s} \dot{V}_{sd} I_{rd} - \frac{L_m}{L_s} (V_{sq} \dot{f}_{n1} - V_{sd} \dot{f}_{n2}) - \frac{L_m V_{sq}}{\sigma L_s L_r} V_{rd} - \frac{L_m V_{sd}}{\sigma L_s} V_{rq} \quad (35)$$

Rewriting (31) and (35) in the form of (17)

$$\begin{bmatrix} \dot{y}_1 \\ \dot{y}_2 \end{bmatrix} = A(x) + E(x) \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} \quad (36)$$

where:

$$A(x) = \begin{bmatrix} \frac{V_{sd}}{L_s} (\dot{\phi}_s - L_m \dot{x}_1) - \frac{L_m}{L_s} \dot{V}_{sq} x_2 - \frac{L_m}{L_s} (V_{sd} \dot{f}_{n1} + V_{sq} \dot{f}_{n2}) \\ \frac{V_{sq}}{L_s} (\dot{\phi}_s - L_m \dot{x}_1) + \frac{L_m}{L_s} \dot{V}_{sd} x_2 - \frac{L_m}{L_s} (V_{sq} \dot{f}_{n1} - V_{sd} \dot{f}_{n2}) \end{bmatrix} \quad (37)$$

$$E(x) = \begin{bmatrix} -\frac{L_m V_{sd}}{\sigma L_r L_s} & -\frac{L_m V_{sq}}{\sigma L_s} \\ -\frac{L_m V_{sq}}{\sigma L_r L_s} & \frac{L_m V_{sd}}{\sigma L_s} \end{bmatrix} \quad (38)$$

The equivalent scheme of MRAC for adjusting stator active and reactive powers is depicted in Fig. 7. The proposed control is described in detail in Fig. 8.

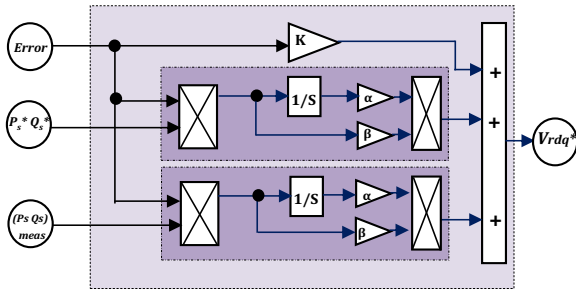


Fig. 7 – The schematic diagram for the proposed MRAC.

Since  $E(x)$  is nonsingular, the control scheme is given from (23) and (24) as:

$$\begin{bmatrix} V_{rd} \\ V_{rq} \end{bmatrix} = +E^{-1}(x) \left[ -A(x) + \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} \right] \quad (39)$$

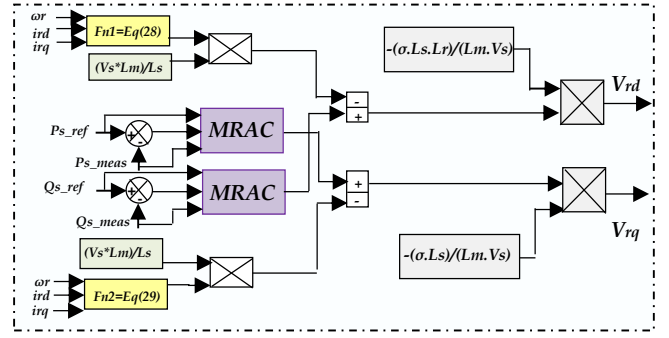


Fig. 8 – Schematic diagram of new input/output linearizing control.

In  $A(x)$  and  $E(x)$ , most components relate to the factors  $L_m/L_s$  and  $\sigma$  that are equal to one approximately, and the functions  $f_{n1}$  and  $f_{n2}$  have no relation with the parameters of the stator windings. Hence, the control law is robust to machine parameter variations.

For the DFIG reference powers, the real reference power  $P_s^*$  is extracted via the WT's MPPT (maximum power point tracking) strategy according to the wind-speed variation, and the requested reactive power  $Q_s^*$  is defined by the network operator to withstand the network voltage. The model reference adaptive controller (MRAC) performs power tracking. Therefore, the MRAC technique is described below.

In this paper, the studied system is defined as a first-order linear approximation [21-24]:

$$\dot{x}(t) = a.x(t) + b.u(t) \quad (40)$$

where  $x(t)$ : is the plant state,  $u(t)$ : is the control signal,  $a$  and  $b$  are the plant parameters. The control signal is generated from both the state variable and the reference signal  $r(t)$ , multiplied by the adaptive control gains  $k$  and  $k_r$  such that:

$$u(t) = k(t)x(t) + k_r(t)r(t) \quad (41)$$

where  $k(t)$ : is the feedback adaptive gain and  $k_r(t)$ : the feed-forward adaptive gain. The plant is controlled to follow the output from a reference model

$$\dot{x}_m(t) = a_m x_m(t) + b_m r(t) \quad (42)$$

where  $x_m$  is the state of the reference model and  $a_m$  and  $b_m$  are the reference model parameters specified by the controller designer. The object of the MRAC algorithm is for  $x_e \rightarrow 0$  as  $t \rightarrow \infty$ , where  $x_e = x_m - x$  is the error signal. The dynamics of the system may be rewritten in terms of the error such that

$$\dot{x}_e(t) = a_m x_e(t) + (a - a_m - b k(t))x(t) + (b_m - b k_r(t))r(t) \quad (43)$$

Using eqs. (41), (42) and (43), it can be seen that for exact matching between the plant and the reference model, the following relations hold

$$k = k^E = \frac{a - a_m}{b} \quad (44)$$

$$k_r = k_r^E = \frac{b_m}{b} \quad (45)$$

where  $()^E$  denotes the (constant) Erzberger gains [30].

Equations (44) and (45) can express eq. (43) as:

$$\dot{x}_e(t) = -a_m x_e + b(k^E - k)(x_m - x_e) + b(k^E - k)r \quad (46)$$

For general model reference adaptive control, the adaptive gains are commonly defined in a proportional plus integral formulation

$$k(e, t) = \int_0^t \alpha y_e (Ps - Qs)_{meas}^T dt + \beta y_e (Ps - Qs)_{meas}^T \quad (47)$$

$$k_r(e, t) = \int_0^t \alpha y_e (Ps - Qs)_{ref}^T dt + \beta y_e (Ps - Qs)_{ref}^T \quad (48)$$

where  $\alpha$  and  $\beta$  are adaptive control weightings representing the adaptive effort.  $y_e$  is a scalar weighted function of the error state and its derivatives,  $y_e = C_e x_e$  where  $C_e$  can be chosen to ensure the stability of the feed-forward block.

In this paper, the proposed MRAC controller also could define as the adaptive controller (generalized definition).

## 5. SIMULATION RESULTS

The simulation results reported in Figs. 9, 10 presents the electrical behavior of the wind-power generation system under variable wind speed. In this context, the parameters of the DFIG (4.0 kW) and wind turbine (4.5 kW) used in the proposed power algorithm are indicated respectively in Appendix.

Figure 9 shows stator real and reactive powers, respectively. It can be seen clearly that the measured powers track exactly their reference with short response time and neglected overshoot. Also, a perfect decoupled power was noted between 0.05 s and 0.35 s. The stator direct and transversal currents ( $I_{sd}$  and  $I_{sq}$ ), respectively, are shown in Fig. 9-c, directly proportional to the reactive and real power ( $Q_s$  and  $P_s$ ). Figure 9-d shows the rotor transversal and direct currents, respectively, which present the inverse curves of stator real and reactive powers. Figure 9-e displays the rotor direct and transversal fluxes, representing the inverse curves of  $Q_s$  and  $P_s$ , respectively. The tracking error of stator real and reactive powers (Fig. 9-f) when various step changes happen. A low power static error is near:  $-55 \text{ W} \leq \Delta P_s \leq +55 \text{ W}$  and  $-55 \text{ VAR} \leq \Delta Q_s \leq +55 \text{ VAR}$ , which means nearly  $\pm 2.5\%$  from rated power.

The stator currents  $I_{s\_abc}$  are presented in Fig. 9-g; from the zoom, the sinusoidal form with few ripples (low THD, nearly 01.41 %) can be seen. Figure 9-h depicts the rotor current  $I_{r\_abc}$ ; the perfect sinusoidal form of the 03 phases rotor currents is also noted, without ripples that prove a good tracking of the rotor quadrature and direct currents (abc/dq Park transformation) exactly which the same manner as the stator active and reactive powers which are imposed by the nonlinear input/output power control. So, it is concluded that the rotor quadrature and direct currents are the variable images of the stator's active and reactive powers, respectively. So, the DMC guarantees the bidirectionality of the power flow, the PF unity, and sinusoidal input/output waveforms. In this work, the DFIG works under  $<1500 \text{ rpm}$  (slip  $S > 0$ ), which means the sub-synchronous modes, when the rotor absorbs the power from the grid ( $P_r = +S * P_n$ ). In the same manner for the frequencies  $f_r = S * f_s$ , the rotor frequency is few than the stator frequency ( $f_r < f_s$ ). To confirm the high wind-system performances of the proposed control, robustness tests are applied as shown below (Table 2): the  $P_s$  and  $Q_s$  are shown in Fig. 10 (a and b, respectively).

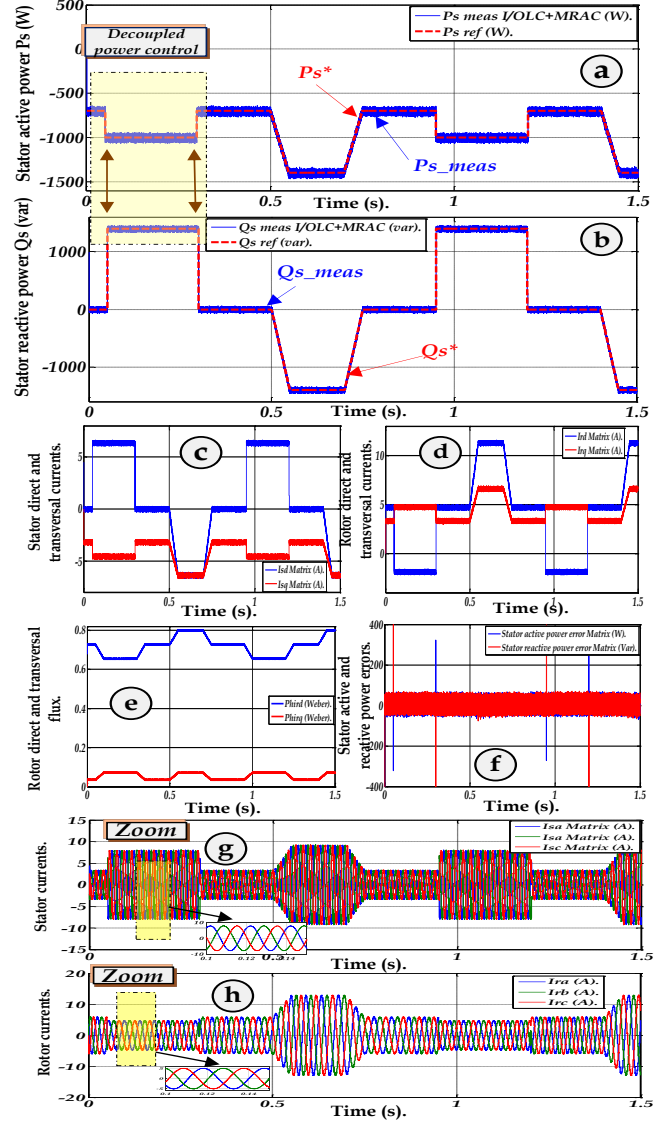


Fig. 9 – (a)  $P_s$ (W), (b)  $Q_s$ (VAr), (c)  $I_{sd}$ (A), (d)  $I_{rd}$ (A), (e)  $\Phi_{rd}$ (Wb), (f)  $\Delta P_s$ (W) &  $\Delta Q_s$ (VAr), (g)  $I_{sbac}$ (A), (h)  $I_{rabc}$ (A).

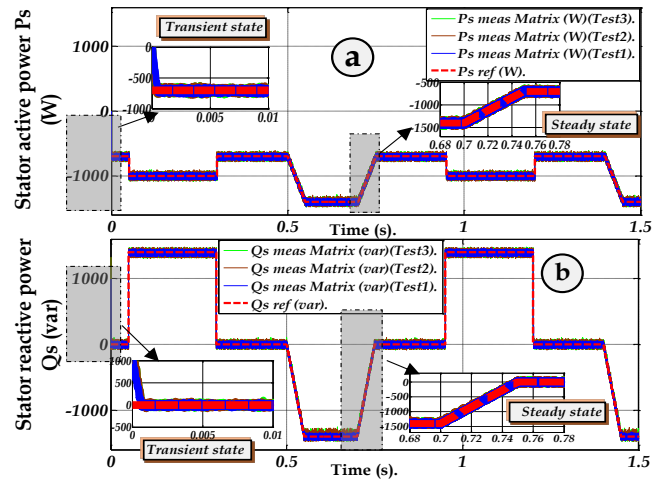


Fig. 10 – Robustness tests with variation of wind system parameters: (a)  $P_s$ (W) and (b)  $Q_s$  (VAr).

It is noted that the stator active power (Fig. 10-a) follows exactly its references (Test-1). After robustness tests (Test-2), a good power tracking is noted with few undulations (zoom) with very short response time nearly 0.002 s for both states (transient and steady). After adding

100 % of moment inertia  $J$  (Test-3), some ripples are noted, especially between 0.55 s and 0.65 s (due to the sudden) with neglected overshoot, especially in 0.3 s and in 0.95 s. The stator reactive power (Fig. 10-b) also follows exactly its reference (Test-1). After robustness tests (test-2), we note perfect power tracking with a very short response time ( $< 0.005$  s for the transient state). After adding 100 % of  $J$ , there can be no overshoot and good power tracking with some ripples between 0.55 s and 0.65 s. The overshoot detection (%), the total harmonic distortion (THD %) of stator currents (from 0.2 s, based on 50 cycles), and THD of rotor currents (from 0.6 s, 20 cycles) and the power errors for the conventional and proposed algorithms are illustrated in Table 3.

Table 2

The robustness tests for the power control.

Test 1:	Without parameters change.
Test 2:	+100% for $R_r$ , -25% for $L_s$ , $L_r$ , and $L_m$ .
Test 3:	+100 % for $R_r$ and $J$ , -25% for $L_s$ , $L_r$ , and $L_m$ .

Table 3

The DFIG power control performances

	Proposed control	Conventional control
The overshoot	$< 1\%$	$< 5\%$
THD (%) of $I_{sabc}(A)$	01.41%	01.42%.
THD (%) of $I_{rabc}(A)$	12.78%	177.83%.
The power static error: $\Delta(P, Q)$ (W, VAR)	+/- 55	+/- 45 .
The response time:	0.000605 s	0.00067 s.

## 6. CONCLUSION

This paper proposes a robust and adaptive DFIG power control for variable speed wind turbines fed by matrix converter. The rotor circuit is fed using a matrix converter (ac/ac), and their IGBTs are controlled via Venturini Technique. In this context, the linearizing power control based on an adaptive controller, "MRAC", offers the best performance, especially in dynamic response and power quality, compared to the conventional vector control. The simulation results obtained using MATLAB/ Simulink® environment demonstrate the feasibility of the proposed algorithm with high wind performances. The experimental validation under dSPACE card of this proposed algorithm presents an excellent perspective for future research works.

## APPENDIX

The DFIG parameters [21-22, 28-29]:

$P_n=4$  kW,  $R_s = 1.2 \Omega$ ,  $R_r = 1.8 \Omega$ ,  $L_s = 0.1554$  H,  $L_r = 0.1558$  H,  $L_m = 0.15$  H,  $V_s = 220/380$  V,  $P = 2$  (pole pairs),  $N_n = 1440$  rpm,  $f_{DFIG} = 0.00$  N.m/s,  $J = 0.2$  kg.m<sup>2</sup>.

The Turbine parameters [21,22, 28,29]:

$P_n=4.5$  kW,  $P=2$  (pole pairs),  $G= 4.15$ ,  $J_t = 0.00065$  kg.m<sup>2</sup>,  $f_t = 0.017$  N.m/s,  $\rho = 1.22$  kg/m<sup>3</sup>.

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